

Kurvendiskussion

S. 77/3e)

$$f(x) = \frac{4+x^2}{x^2-9} = \frac{x^2+4}{(x+3)(x-3)}$$

$$\mathbb{D} = \mathbb{R} \setminus \{-3; 3\}$$

$$f(x) = f(-x) \\ = \frac{4+(-x)^2}{(-x)^2-9} = f(x) \rightarrow \text{achsensymmetrisch}$$

$$f(0) = -\frac{4}{9} \rightarrow P(0 | -\frac{4}{9})$$

$$x^2+4=0 \quad | -4 \\ x^2 = -4 \quad | \sqrt{\quad} \quad \rightarrow \text{keine Nst.}$$

$$\lim_{x \rightarrow \pm\infty} \frac{4+x^2}{x^2-9} = 1 \quad (\text{ZG} = \text{NG})$$

$$\lim_{x \rightarrow 3^+} \frac{4+x^2}{x^2-9} = -\infty \quad \lim_{x \rightarrow 3^-} \frac{4+x^2}{x^2-9} = +\infty$$

Analog für $x \rightarrow -3$

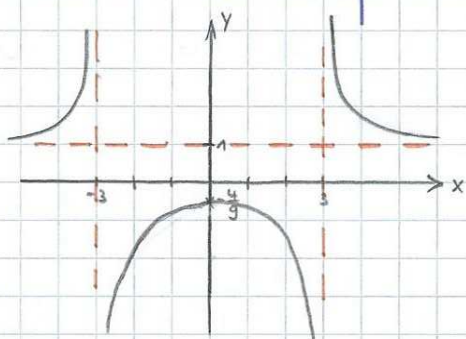
$$u = x^2+4 \quad v = x^2-9 \\ u' = 2x \quad v' = 2x$$

$$f'(x) = \frac{u' \cdot v - u \cdot v'}{v^2} = \frac{2x(x^2-9) - (x^2+4) \cdot 2x}{(x^2-9)^2} = \frac{2x^3 - 18x - 2x^3 - 8x}{(x^2-9)^2} = \\ = \frac{-26x}{(x^2-9)^2}$$

$$-26x = 0 \quad | :(-26)$$

$$x = 0 \rightarrow \text{Extremum}$$

x	$-\infty < x < -3$	$x = -3$	$-3 < x < 0$	$x = 0$	$0 < x < 3$	$x = 3$	$3 < x < +\infty$
f'	+	/	+	0	-	/	-
f	smf	Def. L.	sms	Max. (0 $-\frac{4}{9}$)	smf	Def. L.	smf



$$W =]-\infty; -\frac{4}{9}] \cup]1; +\infty[$$