

b)

$$f(x) = \frac{1}{2}x - \frac{1}{2} + \frac{8}{x+1}$$

 $f(x)$ NEW
 $f'(x)$ NEW
 $f''(x)$ NE

$$f'(x) = \frac{1}{2} + \frac{u' \cdot v - v' \cdot u}{v^2} = \frac{1}{2} + \frac{0 \cdot (x+1) - 1 \cdot 8}{(x+1)^2}$$

$$= \frac{1}{2} + \frac{-8}{(x+1)^2} = \frac{1}{2} - \frac{8}{(x+1)^2}$$

$$f'(x) = 0$$

$$\frac{1}{2} - \frac{8}{(x+1)^2} = 0 \quad | + \frac{8}{(x+1)^2}$$

$$\frac{1}{2} = \frac{8}{(x+1)^2}$$

$$0,5 = \frac{8}{(x+1)^2} \quad | \cdot (x+1)^2$$

$$0,5 \cdot (x+1)^2 = 8 \quad | : 0,5$$

$$(x+1)^2 = 16 \quad | \sqrt{\quad}$$

$$x+1 = \pm \sqrt{16} \quad | -1$$

$$x = \pm \sqrt{16} - 1$$

$$x = \pm 4 - 1$$

$$x_1 = 3 \quad x_2 = -5$$

$$f(3) = \frac{1}{2} \cdot 3 - \frac{1}{2} + \frac{8}{3+1} = 3 \Rightarrow E_1(3|3)$$

$$f(-5) = \frac{1}{2} \cdot (-5) - \frac{1}{2} + \frac{8}{(-5)+1} = -5 \Rightarrow E_2(-5|-5)$$

$$f''(x) = - \frac{0 \cdot (x+1)^2 - 8 \cdot 2 \cdot (x+1) \cdot 1}{(x+1)^4} = \frac{16(x+1)}{(x+1)^4}$$

$$= \frac{16}{(x+1)^3}$$

$$f''(3) = \frac{16}{(3+1)^3} = \frac{1}{4} > 0 \rightarrow E_1(3|3) \text{ Tiefpunkt}$$

$$f''(-5) = \frac{16}{(-5+1)^3} = -\frac{1}{4} < 0 \rightarrow E_2(-5|-5) \text{ Hochpunkt}$$